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PROBLEM SECTION

Edited by Milan J. Merkle

We publish research problems in all areas of Mathematics that fall in one of the following categories:

a) Research problems or conjectures with a solution not known to the proposer.

b) Research problems seeking a new, more elegant solution (the proposer should submit his/her solution).

c) Inquiries about references and state of the art regarding a particular problem.

Problems should be submitted in a form that is easy to understand to a nonspecialist in a field. If using special terms or notations can not be avoided, they should be defined in a statement of a problem. A problem may be accompanied by a short comment (addressed primarily to specialists) that explains why the solution could be of an interest.

Solutions should be worked out in all reasonable details. Solvers should enclose a photocopy of the relevant part of any reference that appears in a solution.

Any solution or an answer to inquiry will be proceeded to the proposer immediately upon receiving.

Correspondence regarding Problem Section should be sent to: Milan Merkle, Faculty of Electrical Engineering, University of Belgrade, P. O. Box 816, 11001 Belgrade, Yugoslavia

• Problem 1.94 proposed by D.S. MITRINOVIĆ, Belgrade.

Let $x \mapsto f(x)$ be a continuously differentiable real function defined on [0, 1]. Suppose that f(0) = 0 and $0 < f'(x) \le 1$ for $x \in [0, 1]$. Find real numbers p and q such that

$$\left(\int_0^1 f(x)\,\mathrm{d}x\right)^p \ge \int_0^1 f(x)^q\,\mathrm{d}x \ .$$

Comment. The inequality holds for p = 2 and q = 3, as indicated in American Mathematical Monthly 81 (1974), 1086-1095.

• Problem 2.94 proposed by D. D. Tošić, Belgrade.

Evaluate
$$\lim_{a \to 0+} \left(\int_{-1}^{1} \frac{\cos x}{x^4 + a^4} \, \mathrm{d}x + \frac{\pi\sqrt{2}}{4a^3} (a^2 - 2) \right).$$

GENERALIZATION. Find the polynomial P_{n-1} with property

$$\lim_{a \to 0+} \left(\int_{-1}^{1} \frac{f(x)}{x^{n} + a^{n}} \, \mathrm{d}x - P_{n-1}\left(\frac{1}{a}\right) \right) = 0,$$

where $z \mapsto f(z)$ is regular function in the disc containing the interval [-1, 1] and $n = 2, 3, \ldots$

Comment. The problem is connected with an expansion of the integral in (1) into LAURENT series with respect to a.

• Problem 3.94 proposed by D.M. MILOŠEVIĆ, Pranjani.

Prove or disprove:

$$\frac{y+z}{x} \cdot \frac{1}{w_a{}^2} + \frac{z+x}{y} \cdot \frac{1}{w_b{}^2} + \frac{x+y}{z} \cdot \frac{1}{w_c{}^2} \ge \frac{18}{s^2} ,$$

where w_a, w_b, w_c are angle bisectors and the semiperimeter of a triangle, and x, y, z are positive numbers.

Comment. The proposed inequality is a generalization of IX.11.1 in D.S. MITRI-NOVIĆ, J.E. PEČARIĆ, V. VOLONEC, Recent advances in Geometric Inequalities, Kluwer, Dordrecht, 1989.

EDITORIAL NOTE

Several readers of our journal have informed us that the paper

B. IRIČANIN: Some quadrature formulas for analytic functions I, These Publications 4 (1993), 105–108.

contains some fallacies in the proof of its main resut. Details will be provided in one of the subsequent issues.